Security of Hedged Fiat-Shamir Signatures under Fault Attacks

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- \cdot Goal
 - Formally analyze the fault-resilience of existing Fiat–Shamir signatures, motivated by actual attacks.
- \cdot Outline
 - 1. Brief history of the fault attacks on FS signatures and randomness hedging.
 - 2. Fault attacker model.
 - 3. Overview of our provable security analysis.

Fiat–Shamir-type Signatures and Attacks

Signature from Canonical ID Protocol

 $\begin{array}{ccc} \operatorname{Prover}(sk;r) & \operatorname{Verifier}(pk) \\ \hline (a,St) \leftarrow \operatorname{Com}(sk;r) & \xrightarrow{a} \\ & \stackrel{e}{\longleftarrow} & e \leftarrow \ensuremath{\mathbb{S}} C_{H} \\ & \stackrel{z}{\longleftarrow} & 0/1 \leftarrow \operatorname{V}(a,e,z,pk) \end{array}$

 If ID is special HVZK and special sound (=Σ-protocol), then SIG := FS[ID] is UF-CMA secure.

Signature from Canonical ID Protocol

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Sensitivity of Per-signature Randomness



- *r* must follow the uniform distribution.
- Otherwise there is an attack!

Randomness Failure in Practice

- Poorly designed RNGs.
- VM resets → same snapshot will end up with the same seed.
- Side-channel leakage.
- and more...



iPhone hacker publishes secret Sony PlayStation 3 key

By Jonathan Fildes Technology reporter, BBC News

③ 6 January 2011

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The PlayStation 3's security has been broken by hackers, potentially allowing anyone to run any software - including pirated games - on the console.

A collective of hackers recently showed off a method that could force the system to reveal secret keys used to load



BBC news. 2011. https://www.bbc.com/news/ technology-12116051

Popular Solution: Deterministic Randomness Generation

 $r \leftarrow \mathsf{RNG}(\cdot)$ $r \leftarrow \mathsf{H}'(sk, m)$

- Hash each message keyed with sk.
- Widely implemented, e.g., in EdDSA, ECDSA, Dilithium, etc.
- However, another practical issue arises...

Deterministic FS is Vulnerable to Faults!

- Fault attack
 - Modifies the internal state of the device.
 - Can be performed remotely (e.g., Rowhammer)
- Many recent fault attacks on FS! [BP16, ABF⁺18, RP17, PSS⁺18, SB18, BP18, RJH⁺19]
- Idea: exploit determinism to rewind the prover (= signer).



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Fault Adversary Type I: Special Soundness Attack

- Query 1: get the legitimate signature (a, e, z) on m.
- Query 2: get a faulty signature (a, č, ž) on the same m, by injecting fault on hash I/O or commitment output.
- Special soundness allows $\mathcal A$ to recover sk !

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- · Second signature relies on correlated randomness $\tilde{r} = r + \Delta!$

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- Seems secure, but no formal analysis so far.

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- Formal attacker model and security notions to capture the corrupted nonces and previous fault attacks.
- Proved that hedged FS schemes in general are (in)secure against certain class of fault attacks.
- Application to concrete instantiations.
 - XEdDSA: Variant of EdDSA used in Signal
 - Picnic2: NIST PQC competition round 2 candidate

Attacker Model and Security Notions

- UF-fCMNA Security
 - UnForgeability against Faults, Chosen Message and Nonce Attacks
 - Models hedged construction and corrupted nonces (inspired by [BPS16, BT16]).
 - Equips the adversary with bit-tampering fault attacks.
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\texttt{flip\_bit}_2(\texttt{0110}\ldots) \rightarrow \texttt{0010}\ldots
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• **set_bit**_{*i*,*b*}(*x*) sets the *i*-th bit of *x* to *b*.

 $\texttt{set_bit}_{4,1}(\texttt{O110}\ldots) \rightarrow \texttt{O111}\ldots$

- Focuses on the single-bit faults, characterizing recent attacks on FS.
- · Models most basic transient fault attackers on data flow, e.g.,
 - CPU register values
 - Data buses
 - Memory cells

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$Exp_{HSIG,H,H'}^{UF-fCMNA}(\mathcal{A})$: UF-fCMNA experiment

- H and H' are modeled as RO.
- + HSIG is UF-fCMNA secure if $\Pr[\text{Exp}_{\text{HSIG},\text{H},\text{H}'}^{\text{UF-fCMNA}}(\mathcal{A}) \rightarrow 1]$ is negligible.

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Provable Security Analysis

UF-KOA $\xrightarrow{\text{special HVZK}}$ UF-fCMNA for $\{f_1, f_5, f_6, f_8, f_9, f_{10}\}$

- UF-KOA (Key Only Attack): \mathcal{A} is not given signing oracle.
- $\cdot ~ \text{UF-KOA} \rightarrow \text{UF-fCMNA}$
 - Simulate the faulty HSign oracle by invoking special HVZK simulator.
 - Non-repeating (message, nonce) is crucial, since otherwise the scheme is deterministic!

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Overview of Our Results

If \mathcal{A} doesn't query the same (m, n) pair more than once

- ✓ secure against single-bit faults.
- X insecure against single-bit faults.
- ★ security only holds for signatures from subset-revealing ID (e.g., Picnic).
- ▲ security only holds for signatures from input-delayed ID (e.g., XEdDSA).

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Intuition: $\{St_i\}$ is resilient to faults since it doesn't rely on sk!

Negative Results

- Fault on H' input $(m, n) \sim$ degenerates to deterministic signature.
- Fault on H' output $r \sim$ directly causes randomness bias.
 - Remark: still better than DSign, as large randomness bias doesn't occur.

Application to Concrete Schemes

XEdDSA

- EdDSA is essentially a deterministic Schnorr.
- XEdDSA = hedged Schnorr.
- More fault resilient than EdDSA/Schnorr!
- Already deployed in Signal protocol.

- Derived from ZKP based on MPC-in-the-head by [KKW18].
- Picnic2 follows FS.
- Underlying ZKP is subset-revealing
 → Hedged Picnic2 has more fault resistance!
- Specification recommends randomness hedging.

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- Proved (in)security of hedged FS signatures against basic faults and corrupt nonces.
- Hedging is provably more resilient than the randomized/deterministic FS, but H' input/output should be protected!
- Open questions
 - Extension to more advanced fault attacker model.
 - Multi-bit/position faults. Partially handled by Fischlin and Günther [FG20] (CT-RSA'20) for generic signatures.
 - Fault within Com, Resp or public parameters.
 - Model for instruction skipping faults.
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 - Lattice signatures from FS with aborts.

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