Crystal Structure of $Ca_2 Na_2 (CO_3)_3$ (Shortite)

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(December 18, 1970)

 $Ca_2Na_2(CO_3)_3$ crystallizes in the orthorhombic unit cell a = 4.947(1) Å, b = 11.032(2) Å, and c = 7.108(1) Å at 25 °C with two formula weights in space-group Amm2. The structure has been redetermined, corrected, and refined to $R_w = 0.025$, R = 0.020 using 684 "observed" x-ray reflections from a single crystal. Corrections were made for absorption and isotropic extinction. In the extinction refinements, r refined to 0.00017(1) cm. The structure consists of Ca_2NaCO_3 layers interleaved with Na(CO₃)₂ layers. The Ca ion is coordinated strongly to nine oxygens, including three CO_3 edges, with Ca. . O distances varying from 2.401(2) Å to 2.576(2) Å. One Na ion is coordinated strongly to eight oxygens, including two CO_3 edges, with Na. . . O distances from 2.429(2) Å to 2.605(1) Å. The other Na ion is coordinated strongly to six oxygens, including one CO_3 edge, at 2.296(1) Å to 2.414 Å, and weakly to a seventh at 3.050(3) Å. One CO_3 group is coordinated to seven cations, the other is coordinated to eight. The CO_3 groups have seemingly maximized their edge sharing with Ca ions rather than Na ions.

Key words: Calcium sodium carbonate; crystal structure; shortite; single-crystal x-ray diffraction.

1. Introduction

As part of a program of studies $[1, 2]^{1}$ to obtain precise structural parameters on calcium carbonates, calcium carbonate hydrates, calcium phosphates, and related compounds, we have reinvestigated the crystal structure of Ca₂Na₂(CO₃)₃, which exists in nature as the mineral shortite. The structural features in these compounds are important in the consideration of possible epitaxial, syntaxial, and substitutional solid solution relationships in the major inorganic phases found *in vivo*.

Shortite was first found [3] in a matrix of montmorillonite clay which also contains pyrite (FeS₂), calcite (CaCO₃), and a carbonate of magnesium in crystals which were too small to be identified. Massive deposits of the commercially important mineral trona (Na₂CO₃ · NaHCO₃ · H₂O) are also found in the vicinity. A crystal structure for shortite has been reported by Wickman [4], who suggested atomic positions on the basis of refractive indices, spatial considerations, and the intensities of the 0kl reflections. We found this structure to contain one incorrect feature. The corrected structure of shortite is reported here.

2. Data Collection and Structure Refinement

The crystal used in the data collection is an approximate sphere, radius 0.112(4) mm, ground from a shortite fragment from mineral sample 105807, National Museum of Natural History, Smithsonian Institution, Washington, D.C. (sample supplied by J. S. White, Jr.). The sphere was mounted on the goniometer head in our usual way [2].

formula (ideal): Ca₂Na₂(CO₃)₃ cell: orthorhombic a = 4.947(1) Å b = 11.032(2) Å c = 7.108(1) Å volume = 387.9 Å³ space-group Amm2; cell contents 2[Ca₂Na₂(CO₃)₃] reciprocal lattice extinctions: k + l = 2n + 1 for hkl; calculated density 2.620 g · cm⁻³; observed density 2.629 g · cm⁻³ [3].

The procedure given in reference [2] was followed in the collection and processing of data with the following exceptions. The θ -2 θ scans were carried out at 2°/min. Each background was counted for 20 s. 1659 reflections were collected from the *hkl* and *hkl* octants and were merged into a unique set of 711, of which 684 are "observed" and 27 are "unobserved." The *R* factor between observed equivalent reflections was 0.01. No absorption corrections were made because the maximum error in an intensity due to absorption is 0.8 percent. For Ca₂Na₂(CO₃)₃, μ (Mo)=15.7 cm⁻¹. The Picker² hardware dropped the least significant

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¹ Figures in brackets indicate the literature references at the end of this paper.

² Certain commercial equipment, instruments, or materials are identified in this paper in order to specify the experimental procedure adequately. In no case does such identification imply recommendation or endorsement by the National Bureau of Standards, nor does it imply that the material or equipment identified is necessarily the best available for the purpose.

digit during the data collection so that the standard deviations from counting statistics, and consequently our assessment of whether a given reflection is observed or unobserved, is only marginally correct. This affects very few reflections in the present case because the sample scattered strongly and nearly all reflections were unequivocally "observed" (modified hardware was used in later investigations). $\sigma(F)$ was defined as F/10 for F < 10; 1 for 10 < F < 43; and F/43 for F > 43, where F_{max} was 211; weights in the least-squares refinements were $1/\sigma^2$. Wickman's structure [4] for $Ca_2Na_2(CO_3)_3$ would not refine to a residual, R_w , below 0.3. Examination of the Patterson function and an F_0 electron density Fourier synthesis phased from structure factor calculations using the positions of the Ca and Na ions suggested new positions for the C(1) and O(1) atoms. This structure was refined isotropically to $R_w = 0.056$, R = 0.050, and anisotropically to $R_w = 0.030$, R = 0.023 and then to $R_w = 0.025$, R = 0.020 with refinement on the isotropic extinction parameter, r, in addition to the previously varied parameters. The least-squares program RFINE written by Finger [5] was used. Only observed reflections were used in these refinements. The scattering factors for the neutral atoms were taken from Cromer and Mann [6]. No corrections for anomalous dispersion were made. The final value of r is 0.00017(1) cm where $F^2 = F_{unc}^2 (1 + \beta r |F_{unc}|^2)^{1/2}$ and F_{unc} is the structure factor uncorrected for extinction. The notation is that of Zachariasen [7]; here r may be related to the average domain size if the crystal is of type II where the extinction is assumed to be governed by spherical domains. The z coordinate of Ca was set equal to zero to define the origin along c. In the final cycle, the average shift/error was 0.01 and the standard deviation of an observation of unit weight,

$$[\Sigma W (F_0 - F_c)^2 / (711 - 50)]^{1/2},$$

was 0.45.

The highest peaks in an electron density difference synthesis calculated at R = 0.03 corresponded to about 0.1 of an electron. The largest correlation coefficients are 0.42–0.44 between the scale factor and the B_{11} , B_{22} , and B_{33} temperature factors of Ca and 0.64 between the extinction parameter and the scale factor. All other correlation coefficients are less than 0.28.

The atomic parameters are given in table 1. All atoms but O(2) lie in special positions; the Wyckoff symbol and symmetry of these positions are given in table 1. The observed and calculated structure factors, uncorrected for extinction, are given in table 2.

3. Description of the Structure

The structure of $Ca_2Na_2(CO_3)_3$ is shown in figures 1 and 2. There are Ca_2NaCO_3 layers at x=0.5 and $Na(CO_3)_2$ layers at x=0. The CO_3 group containing C(2), O(3), O(4), and O(4') lies on the mirror at x = 0.5and is a member simultaneously of three cation-anion chains in which cations are coordinated to edges and opposite apexes of the CO_3 group. One $CaCO_3$ chain runs parallel to [011], one runs parallel to [011], and one NaCO₃ chain runs parallel to [001]. Similar cationanion chains are present in the barytocalcite phase of $BaCa(CO_3)_2$ [8]. The bonding of the apex of the CO_3 group in the NaCO₃ chain to Na is weak, however. The CO_3 group containing C(1), O(1), O(2), and O(2'), which is on the mirror at x=0 and has its plane parallel to (011) or (011), forms NaCO3 chains like those cation-anion chains at x=0.5. The two oxygens O(2) and O(2'), which lie above and below the mirror, provide bonding with cations in neighboring $Ca_2Na(CO_3)$ layers. Each Na at x=0 is common to two chains. The CO₃ groups have seemingly oriented themselves to maximize edge coordination to Ca; each CO₃ group is bonded edgewise to two Ca ions and one Na ion. Preferential edge coordination of CO_3 to Ca is in accord with Ca exerting the largest electrostatic attraction on the CO₃ group and is consistent with the Ca coordinations in CaCO₃ · $6H_2O$ [1], $CaNa_2(CO_3)_2 \cdot 5H_2O$ [9], and $CaNa_2(CO_3)_2 \cdot$ 2H₂O [9].

There is a void in the structure centered at about 0, 0.5, 0.8 (figs. 1 and 2). If the ionic radius of the oxygen in the CO_3 groups is assumed to be 1.4 Å, this void is about 2.2–2.5 Å in diameter. Because it has both cations and anions in its surface, it is unlikely that it would be occupied, except perhaps by an inert gas atom.

TABLE 1. Atomic parameters of Ca₂Na₂(CO₃)₃

Atoms	(")	x	у	z	B *	B_{22}	B ₃₃	B_{12}	B ₁₃	B_{23}
Ca Na(1)	e, m, 4 a. mm, 2	$0.5 \\ 0.0$	$0.21659(4) \\ 0.0$	$0.0 \\ 0.9263(3)$	0.65(1) 1.27(6)	$0.48(1) \\ 0.97(5)$	$0.58(1) \\ 1.54(6)$			-0.01(1)
Na(2)	b, mm, 2	0.5	0.0 0.2961(2)	0.6122(3) 0.1697(3)	1.15(5) 0.57(6)	0.69(5) 0.84(7)	1.15(5) 0.64(5)			-0.04(5)
O(1)	d, m, 4 d, m, 4	0.0	0.2901(2) 0.1985(2) 0.2456(1)	0.0742(3)	1.08(6)	1.35(7)	1.44(7)	0.10/2)	0.04(2)	-0.81(6)
O(2) C(2)	f, 1, 8 b, mm, 2	0.2261(3) 0.5	0.3456(1) 0.0	0.2152(2) 0.2253(5)	0.59(4) 1.1(1)	1.02(4) 0.58(8)	1.08(4) 0.64(9)	-0.19(3)	-0.04(3)	-0.02(3)
O(3) O(4)	$b, mm, 2 \\ e, m, 4$	$\begin{array}{c} 0.5 \\ 0.5 \end{array}$	$0.0 \\ 0.1013(2)$	$0.0415(4) \\ 0.3111(3)$	1.7(1) 2.10(7)	$0.60(7) \\ 0.57(5)$	$\begin{array}{c} 0.61(7) \\ 0.99(6) \end{array}$			-0.23(5)

Figures in parentheses are standard errors in last significant figure quoted, and were computed in the final cycle of full-matrix leastsquares refinement.

" Wyckoff symbol, site symmetry, and multiplicity of site in space-group Amm2.

*Thermal parameters have the form $\exp(-1/4(a^{*2}B_{11}h^2 + b^{*2}B_{22}k^2 + c^{*2}B_{33}l^2 + 2a^{*}b^{*}B_{12}hk + 2a^{*}c^{*}B_{13}hl + 2b^{*}c^{*}B_{13}kl))$.

 $TABLE \ 2. \ Observed \ and \ calculated \ structure \ factors \ for \ Ca_2Na_2(CO_3)_3 \ (short ite)$

0.0.1 2 514 529 186 6 115 517 853 10 251 261 985 6 177 175 833 10 251 261 987 1 299 297 888 1 299 297 888 0 44 39 944 0 44 39 944 0 496 997 12 2 408 490 496 97 1 2 189 129 0 44 39 496 0 40 496 97 1 2 189 128 1 497 396 330 0 391 41 38 5 196 194 59 0 741 138 5 196 194 59 1 173 174 935 0 466 59 07 1 173 174 935 0 466 59 0 466 59 0 466 59 0 471 53 449 0 496 99 0 496 59 0 754 1 147 148 934 0 755 100 2 300 372 819 0 754 148 931 3 497 499 990 0 754 148 934 0 754 70 887 12 128 128 128 23 0 456 59 0	1 1 1 1 1 1 1	1 1/2 1/2 1/2 1/2 1 1/2 1/2 1/2 1/2 1 1/2 1/2 1/2 1/2 1 1/2 1/2 1/2 1/2 1 1/2 1/2 1/2 1/2 1 1/3 1/2 1/2 1/2 1 1/3 1/2 1/2 1/2 1 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2	<pre>5 192 192 101 7 1 1* 21 403 9 70 74 74 1 1* 21 403 9 70 74 74 1 1* 21 403 0 21 74 277 03 6 141 140 988 8 240 248 75 7 115 4 1 33 35 46 7 24 252 267 6 141 140 988 8 240 248 75 7 24 251 251 974 1 35 75 1 16.L 1 35 75 75 2 121 21 974 1 177 175 7 10 77 10 2 143 105 621 7 10 75 75 1 10 71 75 2 10 21 121 977 7 10 77 10 2 10 21 121 977 7 10 77 10 1 107 77 10 2 10 21 10 21 1 107 10 1 1</pre>	11 110 122 943 2010 20	2.18.4 2.19.4 2.19.4 1.19.4	2 2 2 3 3 3 3 3 3 3 1 5 5 1 2 1 2 1 1 2 1 2 1 1 1 2 1 2 1 1 2 1 2 1 1 2 1 2 1 1 1 2 1 1 1 1 2 1 2 1 2 1 2 2 2 2 1 2 1 1 1 1 2 2 1 1 1 2 3 1 1 1 2 1 1 1 1 1 1 1 1 1 1 2 1 1 1 1 2 1 1 1 1 2 1 1 1 1 2 1 1 1 1 3 1 1 1 1 3 1 1 1 1 <t< th=""><th>3 393 306 125 5 7 100 120 120 113 113 134 938 4 40 12 4 13 13 134 938 4 40 12 4 13 13 134 938 4 14 13 134 9 120 135 0 4 140 145 300 4 140 145 300 4 145 30</th><th>**15*L 1 3 5 6 623 5 37 28 623 5 37 28 623 5 37 28 937 **17*L **17*L **17*L 1 326 122 37 5 27 28 937 5 15 500 515 1 326 122 78 5 126 122 819 5 12 121 120 122 5 12 121 120 157 5 12 121 120 127 12 121 120 127 120 12 121 123 123 123 12 121 123 123 123 12 121 123 123 123 5 13 130 123 12 1</th><th>5.10.L 0.16.10, 100, 500 1.17, 103, 103, 103, 103, 103, 103, 103, 103</th><th>8 46 66 858 6.7-L 1 11 11 19 92 5.272 276 60 92 60 92 5.272 276 60 92 60 92 60 92 60 92 60 92 60 92 60 92 60 92 50 93 60 93 51 70 73 71 91 51 71 91 51 71 91 51 71 91 60 6<!--</th--><th>7.66L 0.190 7.500 1.121 1.000 7.71L 1.131 1.131 1.19 1.131 1.19 1.131 1.19 2.192 1.111 2.192 1.111 2.192 1.111 1.111 1.19 2.192 1.111 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14</th></th></t<>	3 393 306 125 5 7 100 120 120 113 113 134 938 4 40 12 4 13 13 134 938 4 40 12 4 13 13 134 938 4 14 13 134 9 120 135 0 4 140 145 300 4 140 145 300 4 145 30	**15*L 1 3 5 6 623 5 37 28 623 5 37 28 623 5 37 28 937 **17*L **17*L **17*L 1 326 122 37 5 27 28 937 5 15 500 515 1 326 122 78 5 126 122 819 5 12 121 120 122 5 12 121 120 157 5 12 121 120 127 12 121 120 127 120 12 121 123 123 123 12 121 123 123 123 12 121 123 123 123 5 13 130 123 12 1	5.10.L 0.16.10, 100, 500 1.17, 103, 103, 103, 103, 103, 103, 103, 103	8 46 66 858 6.7-L 1 11 11 19 92 5.272 276 60 92 60 92 5.272 276 60 92 60 92 60 92 60 92 60 92 60 92 60 92 60 92 50 93 60 93 51 70 73 71 91 51 71 91 51 71 91 51 71 91 60 6 </th <th>7.66L 0.190 7.500 1.121 1.000 7.71L 1.131 1.131 1.19 1.131 1.19 1.131 1.19 2.192 1.111 2.192 1.111 2.192 1.111 1.111 1.19 2.192 1.111 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14</th>	7.66L 0.190 7.500 1.121 1.000 7.71L 1.131 1.131 1.19 1.131 1.19 1.131 1.19 2.192 1.111 2.192 1.111 2.192 1.111 1.111 1.19 2.192 1.111 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.19 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14 1.111 1.14
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Columns are l, $10F_0$, $10F_c$ and phase in millicycles. "Unobserved" reflections are marked by *. The F_c values do not include corrections for extinction. F_0 and F_c are on an absolute scale.



 $\label{eq:FIGURE 1.} \begin{array}{ll} The \ crystal \ structure \ of \ Ca_2Na_2(CO_3)_3, \ short ite, \ viewed \ along \ a. \\ The \ origin \ of \ the \ coordinate \ system \ is \ marked \ by \ ^*. \end{array}$



FIGURE 2. As in figure 1 but viewed along c.

3.1. The Calcium Ion Environment

The Ca ion lies on a mirror plane at x=0.5. Its environment is shown in figure 3 and summarized in table 3. The coordination contains three CO₃ edges, O(1¹, 2¹), O(1, 2) and O(3, 4), and three CO₃ apexes, O(2¹¹), O(2¹¹¹) and O(4¹). The Ca . . . O distances indicate strong ionic bonding from Ca to all these oxygen atoms and are in the normal range. Strong coordination to nine neighboring oxygens is rare for Ca and is possible here because of the small O . . . O separation (~ 2.2 Å) in the edge of the CO₃ group. A large coordination number for Ca is favored by the Ca . . . O interaction being the strongest electro-

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IABLE 3.	The	calcium	environment	ιn	Ca_2N	$a_2($	CO_3)3

Atoms	Distance
$\begin{array}{c} \text{Ca, O(4)} \\ \text{Ca, O(3)} \\ \text{Ca, O(2, 2^{1}, 2^{11}, 2^{111})} \\ \text{Ca, O(1, 1^{1})} \\ \text{Ca, O(4^{+})} \end{array}$	Å 2.401(2) 2.411(1) 2.508(1) 2.543(1) 2.576(2)

In all tables of interatomic distances and angles, the quantities in parentheses are standard errors in the last significant figure and were computed from the standard errors in the atomic positional parameters and in the cell parameters. They include contributions from the variance co-variance matrix. The atom labels refer to atoms in figure 3.



static attraction in the crystal. The Ca ions are about 4 Å apart in the structure; the shortest Ca . . . Na distance, with associated weaker electrostatic repulsion than Ca . . . Ca, is about 3.5 Å.

3.2. The Na Ion Environments

There are two crystallographically distinct Na ions in the crystal structure. Na(2) and Ca lie in the same plane perpendicular to [100]. Na(1) lies halfway between the planes containing Na(2) and Ca. Both Na ions lie at the intersections of mirror planes.

Na(1) is coordinated (fig. 3 and table 4) to eight oxygen atoms, of which $O(2^{111}, 2^{1V})$ and $O(2^{V}, 2^{V1})$ are CO_3 edges. All the Na(1) . . . O distances are within the normal range and indicate strong ionic bonding. The coordination is similar to that of (i) the Ca ion CaNa₂(CO₃)₂ · 5H₂O [9], where the oxygens not in shared edges are in water molecules, and (ii) the Ca(1) ion in Ca₅-(PO₄)₂SiO₄ [10].

TABLE 4. The sodium environments in $Ca_2Na_2(CO_3)_3$

Atoms	Distance
Na(1), O(1, 1 ¹) Na(1), O(2 ¹¹¹ , 2 ^{1V} , 2 ^V , 2 ^{V1}) Na(1), O(3, 3 ¹)	\mathring{A} 2.429(2) 2.530(2) 2.605(1)
Na(2), O(2^{II} , 2^{III} , 2^{VI} , 2^{VII}) Na(2), O(4, 4^{I}) Na(2), O(3)	$\begin{array}{c} 2.296(1) \\ 2.414(3) \\ 3.050(3) \end{array}$

The atom labels refer to atoms in figure 3.

FIGURE 3. The Ca and Na environments in Ca₂Na₂(CO₃)₃. The primes refer to atoms in tables 3 and 4.

Na(2) is bonded strongly to six oxygen atoms (table 4) essentially arranged in a square pyramid with a CO₃ shared edge O(4, 4¹) centered about the apex position (fig. 3). The environment of Na(2) is completed by O(3), which is, however, 3.050 Å away and thus bonded relatively weakly to Na(2). The geometry of strong coordination for Na(2) is like that of Na(2) in Na₂CO₃ · H₂O [11].

3.3 The CO₃ Groups and Their Environments

The dimensions of the CO₃ groups are given in table 5. The C(1) CO₃ group is nearly trigonal with an average C-O distance of 1.282 Å; the C(2) CO₃ group appears to be significantly non-trigonal, but with an average C-O distance of 1.283 Å. The average C-O distances compare well with 1.283(2) Å in calcite (CaCO₃) [12], 1.285 Å in aragonite (CaCO₃) [2], 1.286 Å in Na₂CO₃·H₂O [11], 1.288 Å in CaNa₂ (CO₃)₂·5H₂O [9], 1.286 Å in CaNa₂ (CO₃)₂·2H₂O [9], and 1.286 Å in CaCO₃·6H₂O [1]. All these distances are uncorrected for thermal motion.

The environments of the CO_3 groups are shown in figure 4 and are summarized in table 5. All three edges of both CO_3 groups are coordinated, in both cases to two Ca ions and one Na ion in the same plane as the CO_3 group. All oxygen atoms are further coordinated: O(1) to Na(1) in the plane of the C(1) CO₃ group, O(2) to Ca and Na(2) both out of this plane, O(4) to Ca(1) in the plane of the C(2) CO_3 group, and O(3) to two Na(1)ions which are both out of this plane. Edge coordination of O(3, 4) and $O(3, 4^{I})$ to Ca is expected to decrease the O(3)-C(2)-O(4) and $O(3)-C(2)-O(4^{T})$ angles in accord with Pauling's rule because the $O(4, 4^{I})$ edge of the same CO_3 group is coordinated with weaker electrostatic force to Na(2). This is in accord with the observed O-C-O angles of 118.7(2)° for the Ca coordinated edges and 122.7(4)°, for the Na coordinated edge. Similar effects would be expected in the other CO_3 group, where O(1, 2) and $O(1, 2^{I})$ are coordinated to Ca and $O(2, 2^{I})$ is coordinated to Na. Here the angles, 119.6(1) for the Ca coordinated edges and $120.9(2)^{\circ}$ for the Na coordinated edge are in the right directions from 120°, but are more nearly equal, which suggests that the effect is more complex than this simple reasoning. The average of the distances Ca . . . O(3) and Ca... O(4) is 2.493 Å; that of the Ca... O(1) and

TABLE 5. The Carbonate Anions and Their Environ-
ments Ca₂Na₂(CO₃)₃

Atoms	Distance, Å, or angle deg.
$\begin{array}{c} C(1), O(1) \\ C(1), O(2, 2^{1}) \\ O(1), O(2, 2^{1}) \\ O(2), O(2^{1}) \\ O(1), C(1), O(2, 2^{1}) \\ O(2), C(1), O(2^{1}) \end{array}$	$\begin{array}{c} 1.273(3) \ \mathring{A} \\ 1.286(2) \\ 2.211(2) \\ 2.238(2) \\ 119.6(1)^{\circ} \\ 120.9(2) \end{array}$
$\begin{array}{l} C(2), \ O(3) \\ C(2), \ O(4, \ 4^{\rm I}) \\ C(3), \ O(4, \ 4^{\rm I}) \\ O(4), \ O(4^{\rm I}) \\ O(3), \ C(2), \ O(4, \ 4^{\rm I}) \\ O(4), \ C(2), \ O(4^{\rm I}) \end{array}$	$\begin{array}{c} 1.306(4) \rm{\AA} \\ 1.273(3) \\ 2.218(3) \\ 2.235(4) \\ 118.7(2)^{\circ} \\ 122.7(3) \end{array}$
$O(1), Na(1^1)$ $O(1), Ca, Ca^1$	$\begin{array}{c} 2.429(2) \ {\rm \mathring{A}} \\ 2.543(1) \end{array}$
O(2), Na(2) O(2), Ca ¹¹ O(2), Ca ¹¹¹ O(2), Na(1) O(2), O(2 ¹¹)	$\begin{array}{c} 2.296(1) \\ 2.508(1) \\ 2.508(1) \\ 2.530(2) \\ 2.709(2) \end{array}$
O(3), Ca O(3), Ca ^{IV} O(3), Na(1), Na(1 ¹) O(3), Na(2)	$\begin{array}{c} 2.411(1) \\ 2.411(1) \\ 2.605(1) \\ 3.050(3) \end{array}$
$O(4), Ca^{11}$ O(4), Na(2) O(4), Ca	$\begin{array}{c} 2.401(2) \\ 2.414(3) \\ 2.576(2) \end{array}$

The atom labels refer to atoms in figure 4.

Ca... O(2) distances is 2.526 Å. The difference of 0.03 Å between these average values may account for part of the difference in angles of the O_3 groups because O(3) and O(4) are bonded more strongly to Ca and the O(3), C(2), O(4) angle would then be expected to be decreased more than the O(1), C(1), O(2) angle.

In the absence of hydrogen bonding, the oxygens coordinated most strongly to cations may be expected to have the longest C = O bonds. This is qualitatively the case. Similar effects have been observed in Na₂CO₃ · H₂O [11], CaNa₂(CO₃)₂·5H₂O and CaNa₂(CO₃)₂·2H₂O



FIGURE 4. The environments of the CO₃ groups in Ca₂Na₂(CO₃)₃. The primes refer to atoms in table 5.

[9] and in the PO₄ groups in $Ca_7Mg_9(Ca_5, Mg_2(PO_4)_{12})$ [13]. In the C(1) CO₃ group in Ca₂Na₂(CO₃)₃, the bond distance C(1) - O(2) and the symmetrically equivalent distance $C(1) - O(2^{i})$ are slightly longer than C(1) - O(1). O(2) is coordinated to two Ca ions and two Na ions; O(1) is coordinated to one Ca ion and one Na ion. In the C(2) CO₃ group, C(2) - O(3) is appreciably longer than the two equivalent distances C(2) - O(4) and C(2) - O(4)O(4¹). O(3) is coordinated to two Ca ions and two Na ions; O(4) is coordinated to two Ca ions and one Na ion. The differences in the coordinations of O(3) and O(4) here do not appear large enough to explain the 0.035 Å difference in C-O bond lengths. The difference, 0.020 Å, in the bond lengths C(1) - O(2) and C(2) - O(3), may be partly explained by the fact that while the C(1) CO_3 group has two longer bonds, the C(2) CO₃ group has only one, which may therefore be expected to have approximately twice the extension due to the cation field that the $\dot{C}(1) - O(2)$ bonds have.

The C(1) atom in the C(1) CO₃ group is 0.012(3) Å out of the plane defined by the O(1), O(2), and O(2¹) atoms. This may be a result of perturbation of the sp^2 hybridization of the oxygen atoms by neighboring cations. The C(2) CO₃ group is planar by symmetry.

4. Discussion

The positions given by Wickman, (0.0, 0.226, 0.743)for C(1), (0.0, 0.325, 0.850) for O(1), and (0.230, 0.177, 0.690) for O(2), which are 0.57, 1.98, and 0.31 Å, respectively, from the positions given here, show that in his structure the $C(1)O_3$ group has been reflected along c through the plane z=0.75, so that O(1) then juts out into the void instead of being on the void surface. The interatomic distances are reasonable in Wickman's structure and the O . . . O repulsions are therefore approximately the same in the two models. In the structure reported here, however, O(1) is able to form stronger bonds to the two Ca ions above and below it along a, and to Na(1) in the same plane parallel to (100); this is probably the factor governing the orientation of the CO_3 group. The calculation of refractive indices in the way originally given by Bragg [14] assumes that only oxygen atoms have optical anisotropy and ignores all interatomic interactions. Thus, Wickman, following this procedure, was able to obtain qualitative agreement between observed and calculated values using a model in which the orientation of the C(1) CO_3 group relative to the (001) plane was $\sim 35^{\circ}$ instead of $-31^{\circ} 42'$. The average orientations of C(1) CO₃ groups in the unit cell are about the same for the two models when one takes into account the symmetry operations. This agreement can be seen from table 6, which compares the observed indices with the values calculated for the two models using Bragg's procedure. A much more suitable test of these models, which would produce better quantitative agreement with the observed values, would require consideration of dipole-dipole coupling terms and optical anisotropy of all atoms, especially Na, rather than just oxygens [15, 16]. As a further refinement, the dependence of the atomic optical anisotropy on the environment should be incorporated.

 TABLE 6.
 Refractive indices for shortite

Observed	Wick- man's model	Here	Orienta- tion
$1.531 \\ 1.555 \\ 1.570$	1.515	1.502	c
	1.545	1.541	a
	1.555	1.554	b

J. S. Bowen collected the diffractometer data; P. B. Kingsbury used the ORTEP program of C. K. Johnson, Oak Ridge National Laboratory, to draw the figures. This investigation was supported in part by research grant DE-00572 to the American Dental Association from the National Institute of Dental Research and is part of the dental research program conducted by the National Bureau of Standards, in cooperation with the American Dental Association; the United States Army Medical Research and Development Command; the Dental Sciences Division of the School of Aerospace Medicine, USAF; the National Institute of Dental Research; and the Veterans Administration.

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- 15] Lawless, W. N., and Devries, R. C., Oxygen polarizability and point-dipole theory in the carbonate minerals, J. Phys. Chem. Solids 25, 1119–1124 (1964).
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(Paper 75A2–656)



JOURNAL OF RESEARCH of the National Bureau of Standards – A. Physics and Chemistry Vol. 75A, No. 2, March–April 1971

Publications of the National Bureau of Standards*

Selected Abstracts

Berger, M. J., Seltzer, S. M., Bremsstrahlung and photoneutrons from thick tungsten and tantalum targets, *Phys. Rev. C*, **2**, *No.* 2, 621–631 (August 1970).

Key words: Bremsstrahlung; bremsstrahlung efficiency; Monte Carlo; photon neutron; radiation transport; thick targets.

Monte Carlo calculations have been made of electron-photon cascades in thick tungsten targets bombarded by electrons with energies up to 60 MeV. The following information has been obtained: (1) the bremsstrahlung efficiency, (2) the angular distribution of the emitted bremsstrahlung intensity, (3) the spectra of the bremsstrahlung emitted in various directions, (4) the transmission of primary and secondary electrons through the target, (5) energy deposition as function of the depth in the target, (6) the differential photon tracklength distribution inside the target, and (7) the yield of photoneutrons. The paper also includes various comparisons with experimental data.

Block, S., Weir, C. E., Piermarini, G. J., **Polymorphism in ben**zene, napthalene, and anthracene at high pressure, *Science* **169**, 586–587 (*August* 7, 1970).

Key words: Anthracene; benzene; high-pressure; naphthalene; polymorphism.

High-pressure optical observations using a microscope with the diamond-anvil pressure cell have (1) confirmed that there is a transition in naphthalene and no triple point to $500^{\circ}\pm15^{\circ}$ C, (2) shown that there is a corresponding high-pressure transition in anthracene and no triple point to $550^{\circ}\pm15^{\circ}$, (3) shown that a second reversible high-pressure form of benzene exists with a triple point (liquid-II-III) at $590^{\circ}\pm15^{\circ}$ and approximately 40 kbars, and (4) demonstrated that, at approximately 500° for anthracene, 550° for naphthalene and 600° for benzene III, these materials transform irreversibly to deep reddish-orange colored products which have not yet been characterized.

Bowen, R. L., **Crystalline dimethacrylate monomers**, J. Dental Res. **49**, No. 4, 810–815 (July–August 1970).

Key words: Dimethacrylates; thermosetting monomers; ternary eutectic; urification methods: resins for composites; phthalate monomers; biomaterials.

Certain dimethacrylate monomers can be prepared and purified by recrystallization. Upon mixing, the crystals liquify by forming a ternary eutectic. The colorless oily liquid is suitable for use in composite formulations.

Ensign, T. C., Chang, Te-Tse, Kahn, A. H., **Hyperfine and nuclear quadrupole interactions in copper-doped TiO**₂, *Phys. Rev.* **188**, *No.* 2, 703–709 (*Dec.* 10, 1969).

Key words: Copper; EPR; g-factors; hyperfine interaction; quadrupole coupling; rutile; titanium dioxide.

Single crystals of TiO₂:Cu²⁺ have been investigated at 20 K using the technique of electron paramagnetic resonance. The major features of the EPR spectra can be attributed to divalent copper ($3d^9$) in substitutional (Ti⁴⁺) sites. Information has been gained about both isotopes of copper and about the interactions which concern this ion. For the substitutional site the spin Hamiltonian parameters in the S=1/2, I=3/2 manifold are: $g_x = 2.109$, $g_y = 2.094$, $g_z = 2.346$, $A_x^{63} = +18.7 \times 10^{-4}$ cm⁻¹, $A_y^{63} = +27.2 \times 10^{-4}$ cm⁻¹, $A_z^{63} = -87.5 \times 10^{-4}$ cm⁻¹, $A_x^{63} = +18.8 \times 10^{-4}$ cm⁻¹, $A_y^{63} = +28.7 \times 10^{-4}$ cm⁻¹, $A_z^{63} = -93.7 \times 10^{-4}$ cm⁻¹, $P_x = -2.56 \times 10^{-4}$, $P_y = -2.37 \times 10^{-4}$, $P_z = +4.93 \times 10^{-4}$ cm⁻¹. The magnitudes and relative signs of these parameters have been determined experimentally while the absolute signs have been predicted theoretically from a model which gives a consistent picture of the ordering of the d^9 electronic states. In addition, the theoretical treatment gives a satisfactory estimate of P. Departure from tetragonality was taken into account. The covalency parameter α^2 which measures the fraction of the hole wave function on the Cu²⁺ is found to be 0.71, and κ , the factor giving rise to isotropic hyperfine structure, is found to be 0.31.

Ensign, T. C., Stokowski, S. E., **Shared holes trapped by charge defects in SrTiO**₃, *Phys. Rev. B*, **1**, *No.* 6, 2799–2810 (March 15, 1970).

Key words: Color centers; EPR; hole centers; optical absorption; shared holes; SrTiO₃.

Using the techniques of EPR and optical irradiation in conjunction with optical absorption measurements, we have gained useful information about the nature of some hole centers in SrTiO3. Primarily we have investigated single crystals doped with aluminum at temperatures near 77 K. Two principal centers have been explored: (1) the Al-O⁻ center – a hole shared among the oxygens which surround Al3+, and (2) the X-O- center-a hole shared in a similar fashion, but more deeply trapped by a charge defect of unknown origin. The Al-O- center arises after band gap irradiation and is characterized at 77 K by the following g-values and hyperfine constants: $g_{\parallel} = 2.0137$, $g_{\perp} = 2.0124$, $A_{\parallel} = 8.3 \times 10^{-4}$ cm⁻¹, and $A_{\perp} = 7.6 \times 10^{-4}$ cm⁻¹. The X-O⁻ center is present before optical irradiation. No hyperfine structure is observed, but the isotropic g-value is 2.0130 at all temperatures from 4.2 to 300 K. An 800 nm absorption band arising after band gap excitation has been correlated with the Al-O⁻ center. 430 and 600 nm absorption bands have been correlated with the absence of Fe3+ in the EPR spectrum, and a 500 nm band has also been observed. In addition, the role of iron in the photochronic processes of SrTiO₃ is presented. Finally, theoretical work utilizing the molecular orbital σ and π states in O_h symmetry has provided a firm basis for the sharing model. The experimental g values and hyperfine constants are discussed in light of this mode! and are found to be in good agreement.

Estin, A. J., Editor, Precision measurement and calibration. Selected NBS Papers on electricity-radio frequency, Nat. Bur. Stand. (U.S.), Spec. Publ. 300, Vol. 4, 456 pages (June 1970) 85.50, SD Catalog No. C13.10:300/v.4.

Key words: Admittance; antenna; attenuator: bolometer; calorimetry; horn; impedance; interferometry; measuring system; phase; power; radiometry; resonant cavity; voltage; waveform; waveguide junction.

This volume is one of an extended series which brings together some of the previously published papers, monographs, abstracts, and bibliographies by NBS authors dealing with the precision measurement of specific physical quantities and the calibration of the related metrology equipment. The contents have been selected as being useful to the standards laboratories of the United States in tracing to NBS standards the accuracies of measurement needed for research work, factory production, or field evaluation. Volume 4 contains reprints through June 1967 on radio-frequency electrical measurements covering the following topics: Power, Sinusoidal Voltage and Current, Electromagnetic Fields and Antennas, Radar and Baseband Pulses, Noise, Attenuation and Phase, Impedance, Radio Frequency Materials, Quasi-optics and Millimeter Waves, and Applications to Measurement Systems.

Furcolow, W. H., Technical Standards Coordinator, **Mosaic-parquet** hardwood slat flooring, *Nat. Bur. Stand. (U.S.), Voluntary Prod. Stand.* 27–70, 13 pages (Sept. 1970), 25 cents, SD Catalog No. C13.20/2:27–70.

Key words: Flooring; hardwood flooring; mosaic-parquet flooring: slat flooring.

This Voluntary Product Standard covers requirements for grading, moisture content, dimensions, construction, and finish for mosaicparquet hardwood slat flooring which is intended for use in residential, institutional, and commercial buildings. A method for marking and labeling to indicate compliance with the Standard is also provided. Manufacturers' recommendations on ordering and installation are included in an appendix. The Standard does not cover flooring squares or blocks which are fabricated from conventional tongue and groove type strips.

Goldstein, J. I., Henderson, E. P., Yakowitz, H., Investigation of lunar metal particles (Proc. Apollo 11 Lunar Science Conf., January 1970, Houston, Texas), Geochim. Cosmochim. Acta 1, 499–512 (1970).

Key words: Electron probe microanalysis; lunar samples; lunar simulation: lunar thermal history; meteorites; probe microanalysis; scanning electron microscopy.

Several metallic particles from lunar fine samples 84 and 85-17M and from breccia sample 46-18A were investigated by means of optical microscopy, scanning electron microscopy and electron probe microanalysis. These particles consisted of two large globules, metal spread on glassy spheres, splinters and metal in the foamy pumicelike fragments. The largest globule had a structure consisting of 40 µm Fe-Ni dendrites in a matrix of troilite. A high Ni rim was found at the troilite-dendrite interface. The dendrites showed typical Ni segregation, the composition at the outside being about 16 w/o Ni with 13 w/o Ni at the center. The troilite contained 0.1 to 1.5 w/o Ni and appears to be in dis-equilibrium. The rim contains 29 to 46 w/o Ni and about 0.3 w/o S. The rim is a γ phase in the Fe-Ni-S system and was created by the rejection of Ni from the troilite. We were able to synthesize this globule; the same structure was obtained. From this simulation, the cooling rate was determined as 2.5° C/sec. This globule probably was created by the impact of a chondrite on the moon.

A globule separated from the breccia rock apparently solidified quickly and then cooled slowly, the rock acting as a kind of crucible. This globule's metal regions contain 2 w/o Ni, 1 w/o P, 0.3 w/o Co. balance Fe. There are also phosphide eutectic regions containing fine intergrowths of kamacite, troilite and carbides. This particle shows a striking simularity to spheroids from the Canyon Diablo iron. The evidence indicates that this globule was probably created by the impact of an iron meteorite on the moon.

The analysis of the metal particles makes it clear that both meteoritic and lunar Fe-FeS intergrowth are present in the lunar fines. The lunar metal is similar to the meteoritic material in that it is surrounded by sulfide; both metal constituents are of comparable size, structure and Co content. The two types of material can be differentiated by the significant Ni and P content of the transformed original meteoritic material.

Holt, H. K., Theory of gas lasers and its application to experiment, *Phys. Rev. A*, **2**, *No. 1*, 233–249 (July 1970).

Key words: Collisions: gas laser; line widths; power output: theory: tuning curves.

The semi-classical theory of gas lasers has been reformulated using rate equations to describe the density matrix time behavior. The solution to these equations, in the form of a Fourier series, is applicable to arbitrarily high laser intensities. A calculation of the effect of phase-changing collisions is also included. The results are compared to experimental data taken with a He-Ne laser operating at a wavelength of 1.15 μ m.

Klein, R., A field emission study of carbon monoxide on h.c.p. metals rhenium and ruthenium, *Surface Sci.* 20, *No. 1, 1–17 (March 1970).*

Key words: Carbon monoxide: desorption; field emission; monoxide; rhenium, ruthenium, surface migration.

The surface migration, work function increments, and desorption of carbon monoxide on two h.c.p. metals, rhenium and ruthenium, were observed with field emission techniques. Carbon monoxide is weakly bound to ruthenium and more strongly bound to rhenium. For a complete monolayer, the work function increment is 1.3 eV for ruthenium and 0.8 for rhenium. Surface migration commences at a readily observable rate at about 125 K for ruthenium and shows both boundary and boundary free characteristics. Rhenium has an ill defined surface migration temperature region because the desorption precedes and overlaps it. Two well defined binding states for CO on rhenium are seen.

Ledbetter, H. M., Reed, R. P., **On the martensite crystallography** of Fe-Ni alloys, *Mater. Sci. Eng.* 5, *No.* 6, 341–349 (*June* 1970).

Key words: Crystallographic theory: iron-nickel alloy; martensite.

For the first time lattice parameter data and habit plane measurements are available for an alloy system whose crystallographic features change continuously with composition. This information has been produced for the plate-like martensitic transformation in Febase alloys containing between 29 and 35 wt. % Ni. This paper presents a critical examination of the data from the viewpoint of the theories of martensite crystallography. It is found that the current theories cannot explain the variation of the habit plane with composition without invoking a varying δ (1.000 to 1.013), δ being an isotropic dilatation parameter. In addition to the habit plane, several quantities have been calculated as a function of composition: the volume change, the magnitude of the lattice invariant deformation, the magnitude and direction of the shape change, and the orientation relationship. The effects of errors in lattice parameter and of thermal expansion are considered.

Mann, W. B., Garfinkel, S. B., Editors, **Radioactivity calibration** standards, Nat. Bur. Stand. (U.S.), Spec. Publ. 331, 120 pages (August 1970) \$1.25, SD Catalog No. C13.10:331.

Key words: Alpha-particle standards: calibration consistency; coincidence counting; decay-scheme effects: efficiency tracing; gammaray standards; international comparisons; liquid-scintillation counting; radionuclide half-lives; radionuclide standards.

Experimental procedures and methods used in nine international radioactivity standardization laboratories are described by eight authors. The possibility of attaining accuracies of the order of 0.01 percent are discussed. The desirability of carrying out consistency checks of gamma-ray standards with time, using a $4\pi\gamma$ ionization chamber is emphasized. The validity of radioactivity standards is examined. International comparisons organized by the Bureau International des Poids et Mesures are discussed. An analogue method of liquid-scintillation counting is described. Certain types of radioactivity standards are criticized. The fields of interest of the two Canadian laboratories are discussed. Details of the work in progress at the Boris Kidrič Institute and National Bureau of Standards are presented.

Milligan, D. E., Jacox, M. E., Spectra of radicals in Physical Chemistry, 4, Chapter 5, 193–231 (Academic Press Inc., New York, N.Y., 1970).

Key words: Electronic spectrum; flash photolysis; free radicals: matrix isolation; molecular orbitals; vibrational spectrum.

Problems arising in the direct spectroscopic detection of free radicals are surveyed. Apparatus used for the spectroscopic study of free radicals in the gas phase and trapped in inert solid matrices is described. The advantage and limitations of flash photolysis and of matrix isolation studies for the production and detection of free radicals are considered. Examples of radicals studied by these techniques are cited, and data on the structure and chemical bonding of these species derived from the observed spectra are correlated with the predictions of simple molecular orbital theory.

Reimann, C. W., Santoro, A., Mighell, A. D., **The crystal molecular structure of hexapyrazolenickel(II) nitrate**, Ni(C₃H₄N₂)₆ (NO₃)₂, Acta Cryst. B26, Part 5, 521–526 (May 1970).

Key words: Inorganic coordination complex; octahedral coordination; pyrazole; trigonal symmetry; x-ray structure determination.

The crystal structure of hexapyrazolenickel(II) nitrate, Ni(C₃H₄N₂)₆ (NO₃)₂, was determined by single-crystal diffraction techniques. Crystals of Ni(C₃H₄N₂)₆(NO₃)₂ are trigonal with a = 9.958, c = 7.278Å, space group = P3, Z = 1, $\rho_0 = 1.57$ g, cm⁻³, $\rho_c = 1.57$ g, cm⁻³. Three-dimensional counter data were collected (1115 reflections) and the structure was solved by an analysis of the Patterson map. The complex cation. Ni(C₃H₄N₂)₆⁺, formed by the coordination of six planar pyrazole molecules to the nickel ion, has 3 point symmetry. The nickel ion lies at the center of a nearly regular octahedron of coordinated nitrogen atoms. These complex cations and nitrate anions are linked by hydrogen bonds between each pyrrole type nitrogen atom (N—H) in the pyrazole ring and an oxygen atom in the nitrate group. The final refinement by full matrix anisotropic least-squares analysis resulted in an *R* value of 0.053.

Ruff, A. W., Jr., Measurement of stacking fault energy from dislocation interactions, *Met. Trans.* 1, *No.* 9, 2391–2413 (Sept. 1970).

Key words: Dislocations; dislocation nodes; dislocation ribbons; faulted dislocation dipoles; stacking fault energy: stacking fault tetrahedra.

The theories and methods applied to the determination of the stacking fault energy (γ) using techniques of direct observation of dislocation configurations are reviewed. The four principal methods, utilizing dislocation nodes, multiple ribbons, stacking fault tetrahedra, and faulted dipoles, are discussed in detail. Different theoretical treatments are compared wherever possible. Experimental procedures and quantitative measurement methods are reviewed. Detailed examples of the application of each method are given. For $\gamma/\mu b$ in the range of 2×10^{-4} to 5×10^{-3} (μ the shear modulus, b the Burgers vector), measurements on dislocation nodes or multiple ribbons in favorable cases should permit determinations of the stacking fault energy to a precision of 5 percent. For larger values of $\gamma/\mu b$ (up to 12×10^{-3}), measurements can be made on tetrahedra or faulted dipoles with less precision. Larger values of the stacking fault energy require high resolution studies of dislocations; these techniques are not yet well established. Possible sources of systematic bias are discussed. Two significant theoretical problems remain concerning the treatment of the dislocation core and the use of anisotropic elasticity. It is of prime importance to characterize as carefully as possible the materials studied if accurate results are desired.

Simson, B. G., Mandel, J., Brenner, F. C., Research for a uniform quality grading system for tires. III. Breaking energy, *Rubber Chem. Tech.* 43, *No.* 2, 356–369 (March 1970).

Key words: Bias ply; breaking energy; passenger car; radial; tire strength; tires; winter.

A test procedure, designed to classify tires according to their average breaking energy has been applied to a sample of passenger car tires. Data are reported on 127 different tires of all grades and types over a range of sizes.

A scaling system is devised and applied to the data. It is found that the system leads to conclusions similar to those derived from the original data.

Ugiansky, G. M., Skolnick, L. P., Stiefel, S. W., **Directional effects** in the stress corrosion cracking of an aluminum alloy, *Cor*rosion 25, No. 2, 77–86 (February 1969). Key words: Aluminum alloy; corrosion; directional effects; grain morphology; preferred orientation; stress corrosion.

Studies of the relative effects of grain morphology and preferred orientation on the directional susceptibility to intergranular stress corrosion cracking of a 7075-T651 aluminum alloy plate have been conducted. The role of grain morphology was found to be of paramount importance in controlling crack propagation. It was found that a slow rate of propagation along grain boundaries parallel to the applied stress, and the fact that the intergranular crack must propagate primarily in this direction accounts for the low susceptibility of longitudinally stressed specimens. The results suggest that the threshold stress for short transverse specimens approximates the low stress necessary to crack grain boundaries normal to the applied stress, and the threshold stress for longitudinal specimens approximates the high stress needed to propagate cracks along boundaries parallel to the applied stress. Preferred orientation was found to be of secondary importance when compared to the effect of grain morphology. A high degree of preferred orientation, rather than any specific slip plane orientation, was found to increase the susceptibility of specimens with the same grain morphology. Pitting corrosion was found to occur to a much greater extent on unstressed than on stressed (undergoing stress corrosion cracking) specimens. This phenomenon is explained by what is termed an "internal cathodic protection mechanism."

Wall, L. A., Flynn, J. H., Straus, S., Rates of molecular vaporization of linear alkanes, J. Phys. Chem. 74, 17, 3237–3242 (1970).

Key words: Alkanes; heats; *n*-hexatricontane; *n*-pristane: *n*-tetracosane; *n*-tetranonacontane, vaporization.

The rates of molecular vaporization of four linear alkanes, *n*-pristane (C_{19}) , *n*-tetracosane (C_{24}) , *n*-hexatricontane (C_{36}) , and *n*-tetranonacontane (C_{94}) was measured. By both isothermal and nonisothermal methods, the kinetics of the vaporization process showed essentially zero order behavior as a vaporization process proportional to the surface area should. The Arrhenius slope plus 3 *RT*/2 was compared to heats of vaporization of other *n*-alkanes in the literature. The old and new data show that the heat of vaporization is proportional to the two-thirds power of the number, *n*, of carbon atoms in the species and not to the first power. The majority of the known heats of vaporization, were well fitted by the equation,

$$\Delta H_v = 13.43 \ n^{2/3} - 0.08075 \ T + 12.22, \ \text{KJ/mol}$$

The tetranonacontane vaporized without detection of hydrocarbon decomposition products by mass spectral monitoring. The results suggests a much higher limit to the size of species capable of molecular vaporization without decomposition, than previously assumed.

West, E. D., Churney, K. L., **Theory of isoperibol calorimetry** for laser power and energy measurements, *J. Appl. Phys.* 41, *No.* 6, 2705–2712 (May 1970).

Key words: Calorimetry: laser calorimetry; lasers; thermadynamics.

Laser power and energy measurements are commonly made in calorimeters operating in a constant-temperature environment. These calorimeters are analyzed in terms of the first law of thermodynamics and the boundary value problem describing heat flow in the calorimeter. This theory of the measurement suggest design features of the calorimeter, sources of error to be avoided in design and operation, and tests to demonstrate experimentally the adequacy of the design. The analysis shows how time-temperature data can be used to allow for the temperature gradient on the calorimeter and the heat exchange due to transients in the temperature.

Other NBS Publications

- J. Res. Nat. Bur. Stand. (U.S.), 74C (Eng. and Instr.), Nos. 3&4 (July-Dec. 1970), SD Catalog No. C13.22/sec.C:74/ 3&4. \$1.25.
- Techniques for comparing four-terminal-pair admittance standards. R. D. Cutkosky.

- Some applications for series impedance elements in radio frequency immittance measurements. L. E. Huntley.
- A pulse heating method for the measurement of melting point of electrical conductors (thin wires) above 2000 K. A. Cezairliyan.
- A time-shared computer system for diffractometer control. H. A. Alperin and E. Prince.
- Tensile deformation of vapor-deposited copper reinforced with tungsten wires. W. D. Jenkins, W. A. Willard, and D. A. Harne. "Connector-pair" techniques for the accurate measurement of two-
- terminal low-value capacitances. A. Millea.
- The use of dew-point temperature in humidity calculations. A. Wood, Bolovac application for HF and microwave power measurement and standardization. M. C. Selby.
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- Index to volume 74C, January-December 1970.
- Borie, E., Radiative corrections to back scattering, Phys. Rev. C, 2, No. 2, 770-771 (August 1970).
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