

# ProvenanceMatrix: A Visualization Tool for Multi-Taxonomy Alignments

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**Abstract.** Visualizing and analyzing the relationships between taxonomic entities represented in multiple input classifications is both challenging and required due to recurrent new discoveries and inferences of taxa and their phylogenetic relationships. Despite the availability of numerous visualization techniques, the large size of hierarchical classifications and complex relations between taxonomic entities generated during a multi-taxonomy alignment process requires new visualizations. This paper introduces *ProvenanceMatrix*, a novel tool allowing end users (taxonomists, ecologists, phylogeneticists) to explore and comprehend the outcomes of taxonomic alignments. We illustrate the use of *ProvenanceMatrix* through examples using taxonomic classifications of various sizes, from a few to hundreds of taxonomic entities and hundreds of thousands of relationships.

**Keywords:** Taxonomic classification, multi-taxonomy alignment, phylogenetic relationship, matrix representation, glyph-based visualization

## 1 Introduction

Visualization tools developed for the field of biological taxonomy (herein broadly defined to include phylogenetics) may focus on representing the information content of one comprehensive classification, or provide visual information on the relationships between taxonomic entities represented in multiple, alternative classifications [9, 11]. The latter visualization services are useful in particular for illustrating important similarities and differences in taxonomic perspective, which may be empirically rooted in the discovery of new taxonomic entities, new evidence of phylogenetic relationship, or in the differential sampling and weighting of phylogenetic evidence [10]. Such multi-taxonomy comparisons can be viewed as a solution to the challenge of representing *taxonomic provenance* [11], i.e., linking a taxonomy  $T_1$  to another (pre- or postceding) taxonomy  $T_2$ . To achieve this, taxonomic concepts endorsed by each alternative classification are individuated using taxonomic concept labels with the syntax: *taxonomic name sec. (according to) taxonomic source* [8]. Linkage of same-sourced concepts via parent-child (*is-a*) relationships permits the assembly of multiple independent classifications, and therefore presents new opportunities for inferring and visualizing taxonomic provenance across multiple classifications.

Here we describe *ProvenanceMatrix*, a novel tool for visualizing some of the knowledge products of EULER/X, a multi-taxonomy alignment toolkit [1]. EULER/X is

a logic-based reasoning software capable of aligning (or “merging”) two or more taxonomic concept hierarchies, using different underlying inference mechanisms, in particular, answer sets [12] and qualitative reasoning using RCC-5 constraints [15]. The reasoning process models taxonomies  $T_1$  and  $T_2$  as sets of *is-a* constraints, together with a set  $A$  of expert-asserted input *articulations* that relate concepts in  $T_1$  with those in  $T_2$ , typically at the leaf level. Using RCC-5 (Region Connection Calculus) relations, the expert can express through the articulations in  $A$  which relation holds between a concept  $T_1.X$  and a concept  $T_2.Y$ , i.e., *equals*, *includes*, *is\_included\_in*, *overlaps*, or *disjoint*. If the precise relationship is not known, then one of the non-elementary  $2^5 = 32$  disjunctive combinations of the 5 base relations can be used to express this uncertainty [17].

Fig. 1(a) shows two input taxonomies and the expert articulations. The alignment (or merge) result is depicted in Fig. 1(b). Further below (e.g., see Fig. 4), we propose to replace this view with a more dynamic *ProvenanceMatrix* view, juxtaposing concepts of  $T_1$  (as rows) and of  $T_2$  (as columns). In principle, we could also do this for the input data in Fig. 1(a), but it is primarily the alignment result in Fig. 1(b) that a user will want to visualize and explore.

The toolkit workflow iteratively guides the expert user towards identifying sets of input articulations that are both logically consistent and sufficiently specific to yield only a limited number of consistent alignments [2]. An important product of the alignment process is the set of *Maximally Informative Relations* (MIR): for any pair  $(C_1, C_2)$  of concepts from  $T_1, T_2$ , the MIR of  $(C_1, C_2)$  is the unique relation in the powerset lattice  $R_{32}$  over the RCC-5 base relations which implies all other relations that hold between  $C_1$  and  $C_2$ , given  $T_1, T_2$  and  $A$ .

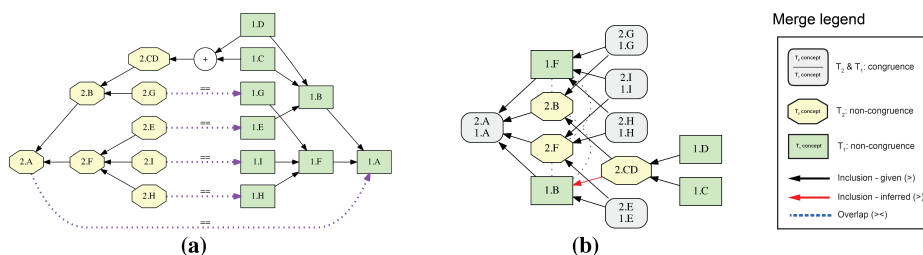
The MIR play a critical role in generating the set of consistent alignments (“possible worlds”), in diagnosing undesired ambiguities in the input or output articulations, and generally in understanding the toolkit reasoning outcomes. Visualization tools are important in this context because the number of MIR for two taxonomies with  $m$  and  $n$  concepts, respectively, is  $m \times n$ . For instance, the alignment use case of *Primates sec. Groves (1993; T<sub>1</sub>)* and *Primates sec. Groves (2005; T<sub>2</sub>)* contains  $317 \times 483$  taxonomic concepts and hence 153,111 MIR relations [11]. Displaying the MIR in list format is not an effective method for exploration. Instead users need dynamically rendered, scalable visualization solutions to navigate the large and semantically complex reasoning outcomes and adjust the input accordingly to achieve the desired alignments.

Key visualization challenges for multi-taxonomy alignment outcomes include the following scenarios. Frequently the alternative taxonomies have unequal sets of leaf-level children. For instance, recently published taxonomies may include new species-level concepts for which there are no corresponding entities in preceding classifications [9]. Additionally, the visualization must display large numbers of data points ( $> 150,000$  in the medium-sized Primate use case), where each point can be constituted by any subset of RCC-5 articulations in the  $R_{32}$  lattice. In order to empirically assess the reasoner-inferred articulations, users may also need to access taxonomic provenance information such as feature-based diagnoses, illustrations, and other taxonomic information.

Using *ProvenanceMatrix*, we can visualize alignments of large taxonomies with up to hundreds of concepts. Our technique uses matrix representation and glyphs in each cell to highlight RCC-5 articulation sets and alignments. In Section 4, we demonstrate how our technique effectively facilitates the exploration of multi-taxonomy alignments with varying sizes and levels of alignment ambiguity.

## 2 Related Work

An overview of the EULER/X multi-taxonomy alignment approach is provided in [9]. Fig. 1 shows the current visualizations of two related concept taxonomies, plus articulations among the respectively entailed taxonomic concepts. The aim is to visualize the input taxonomies  $T_1$  and  $T_2$  and the resulting merged visualizations (rendered with GraphViz [6]). In the figure, “=” means equals, “<” means is\_included\_in, “>” means includes, “><” means *overlaps*, and “|” means disjoint. The final product is a merged taxonomy (as depicted in Fig. 1(b)) that represents the concept-level similarities and differences among the aligned input trees. However, current GraphViz visualizations are not interactive and do not facilitate efficient exploration of ambiguous (under-specified) articulations which generate multiple possible world solutions. Resolving ambiguity is a critical aspect of the alignment process.



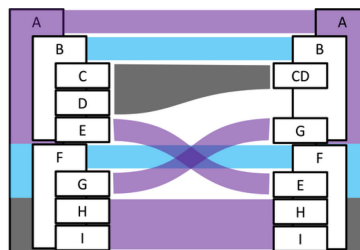
**Fig. 1.** Abstract toolkit input and output example rendered with GraphViz: (a) Representation of two input taxonomies  $T_1$  (left) and  $T_2$  (right) and articulations in the toolkit input file. (b) Single, consistent alignment of the input shown as a containment with overlap graph.

Tanglegrams are widely used in biology, for instance to represent the inferred evolutionary histories of rooted phylogenetic networks [16] and to highlight common structures as well as differences in multiple DNA sequences [18]. A tanglegram draws two rooted trees with the leaves opposing each other and uses auxiliary lines to connect matching taxonomic entities at the leaf-level. These auxiliary lines can be rendered in different styles or colors to encode different types of relationships (e.g., host-parasite associations).

The *Concept Relationship Editor* [3] extends the alignment process to support assertions of relationships between taxonomic classifications at all levels of each aligned hierarchy. *Concept Relationship Editor* adopts a space-filling adjacency layout which allows users to expand multiple lists of taxonomic concepts with common parents. The

lens mode and scroll mode are two different ways to navigate across the hierarchy of either classification while ensuring that the text strings in focus remain legible. Lines are used to connect the related taxa with symbols at either end to indicate the relationship type. Similar to tanglegrams, this technique can introduce visual clutter due to edge crossings as the number of taxa increases.

An alternative visualization approach utilizes icicle tree representations [14]. The RCC-5 relationships are colored bands to connect pairs of taxonomic concepts. Neighboring bands of the same color are bundles that reduce cognitive load. Spaces between concepts of one taxonomy may be used to better align the two trees and reduce crossed bands. In addition, nodes may be color-coded to indicate what percentage of a node’s descendants are congruent or not. Figure 2 shows an example of the icicle tree representation. In the diagram shown, purple means *equals* or congruent ( $=$ ), black means *is included in* or subset ( $<$ ), blue means *overlaps* ( $><$ ). However, this technique is only suitable for smaller numbers of concepts or aggregate views of large classifications. When we try this technique on a large number of taxonomic concepts, and especially when multiple articulations between paired concepts must be displayed, the visualization becomes cluttered due to band crossings.



**Fig. 2.** An example of the icicle tree representation and colored bands to highlight articulations between pairs of taxonomic concepts. (credit Michael McGuffin)

### 3 Design Motivation

In this section, we review the primary challenges inherent in displaying RCC-5-based, multi-taxonomy alignments. Addressing these challenges has motivated us to create a new visualization technique that better supports the visual exploration tasks relevant to such taxonomic reasoning products.

The EULER/X input (constraint) and output (alignment) visualizations as depicted in Figure 1 present slightly different sets of challenges. They are currently produced by toolkit-native stylesheets that translate the user input and reasoner output into GraphViz-compatible data files. While there is some limited flexibility in tweaking the GraphViz output using EULER/X stylesheet options<sup>1</sup>, the ranked graph layout computed by GraphViz may not reflect the user’s intuitions regarding the spatial arrangement of concepts and relationships. For example, the ordering of children of a parent concept computed by GraphViz is different from the order in which they appear in the source publications for that taxonomy. This can create unintuitive experiences for the user.

Smaller scale visualization enhancement goals is improving usability for annotating/editing the GraphViz output data files. Larger scale goals entail acquiring the ability

<sup>1</sup>The stylesheet options result in different GraphViz attribute settings, e.g., “constraint=false” ignores certain edges for layout purposes.

to export/edit EULER/X visualizations in other (phylo-visualizing) platforms (however, a related challenge is that the most popular programs may not support EULER/X semantics which mandate the use of taxonomic concept labels, parent/child relationship [same taxonomy], RCC-5 relationships [across taxonomies], and merge concepts labels [AB, Ab, aB]).

Here, we provide an overview of some of the main visualization tasks for visualizing related concept taxonomies (hierarchies), as well as the relations between the concepts in the input taxonomies. Given two or more taxonomies:

**T1.** Focus on specific articulations.

**T2.** Provide different ways to organize hierarchies. This helps to compare structure of the input taxonomies.

**T3.** Highlight taxonomic concepts in one classification that stand in various specific and incongruent relations to concepts in the other classification.

**T4.** Find related concepts and subtrees of one taxonomic classification to the other taxonomic classification.

**T5.** Display details on demand. In particular, users want to be able to overlay distinctions between user-provided and toolkit-inferred articulations (i.e., articulation source), and display additional domain-relevant information (such as characters, images) when mousing over a concept label.

**T6.** Collapse and expand a subtree to simplify or fully explore a branch. This feature is particularly useful when dealing with large taxonomies.

## 4 Methods

Matrix representation is a useful tool for visualizing networks in many application domains, such as protein-protein biological interactions [5] and social networks [7]. This technique is superior to using node-link diagrams when the networks are dense, given that edge-crossings are the main limitation of node-link diagrams in visualizing these networks. A drawback of matrix representation is the inability to represent the flow of the networks [4]. However, since network flow is irrelevant in multi-taxonomy alignments, we found matrix representation to be best suited for visualizing the data products discussed above. Moreover, matrix representation enables the display of multiple (dis-junct) relationships that may exist between a pair of elements from both dimensions in a matrix [5].

Figure 3 shows an example of *ProvenanceMatrix* for the *Perelleschus* classifications [9]. Each side of the matrix displays an input taxonomy. The arcs are used to indicate hierarchical information, directed from parent to subordinate child concepts. MatLink [13] also uses arcs to indicate relationships but only considers undirected networks. Moreover, the taxonomic concept labels are also indented appropriately to highlight hierarchical arrangement of each input classification. In each cell of the matrix we use circular sectors, divided similarly into a pie-chart, to indicate the articulations that hold true between two taxonomic concepts, where each sector (pie-slice) in the circle is given a color to consistently indicate the articulation type. The more pie-slices are shown, the less we know about the pair of concepts. Thus, a “full circle” (with all 5 pie-slices) means we know nothing about a relation. These “full circle” can act as “alerts”

to the user that the alignment is problematic (too ambiguous). Conversely, a single slice is the best case, specifying a unique (fully specified) relationship between two concepts. Color legend is depicted on the right of Figure 3. For example, green represents *equals* and blue represents *includes*. We use the same color coding for articulations in the the rest of this paper. Users can enable or disable an articulation type as desired (T1).

*ProvenanceMatrix* supports three ways of ordering taxonomic concepts, designed to highlight different aspects of the input hierarchies as well as their RCC-5 articulations. (1) Ordering the matrix with respect to the structure of the input trees. Figure 4 shows *ProvenanceMatrix* with different orderings of taxonomic concepts (T2). (1.1.) Breadth-first ordering in Figure 4(a) lists all sibling together before diving into their respective child-level concepts. (1.2.) Depth-first ordering in Figure 4(b) lists the children right after each taxonomic concept. The hierarchy is more readable in this ordering since there are no crossing arcs in the same taxonomic classification. To avoid the overlapping between arcs and glyphs in the matrix, we can replace arcs by straight lines connecting parent to child concepts. (2) In Figure 4(c), we order the taxonomic concepts based on the similarity of their articulation sets. (The details of how we compute similarity and the ordering algorithm are described in [5].) This ordering brings concepts with multiple alignments to the top left corner of the matrix; these multiple alignments generate the 160 possible worlds in the taxonomy alignment of Gymnospermae sec. Weakley (2010) versus RAB (Radford, Ahles and Bell) (1968) [9]. The example shows ambiguities in the multi-taxonomy alignment which our visualization software can readily identify and isolate to facilitate user-mediated diagnosis and resolution of such ambiguities. In addition, congruent relations (in green) are pushed further to the bottom right of the matrix.

Due to the discovery and/or inclusion of new taxonomic entities in the later (2010) classification, the alternative taxonomies have unequal sets of leaf-level children. In other words, recently published taxonomies may include new species-level concepts for which there are no corresponding entities in preceding classifications. Accordingly, in *ProvenanceMatrix*, we classify taxonomic concepts into three different categories (T3):

- Neither the concept nor any of its children of one taxonomy have congruent relationships with entities in the other taxonomy. In other words, a (set of) concept(s) has no match whatsoever (“bad apples”). Such concepts are highlighted in red in Figure 5.
- A parent-level concept is incongruent but entails one or more congruent child-level concepts. In other words, the higher-level concepts is a unique conglomerate of

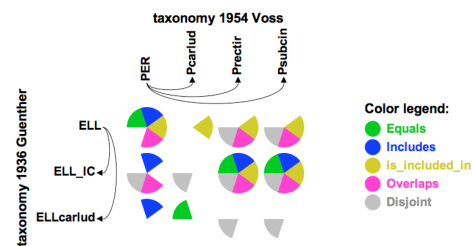


Fig. 3. An example showing the use of *ProvenanceMatrix* for the *Perelleschus* classifications.

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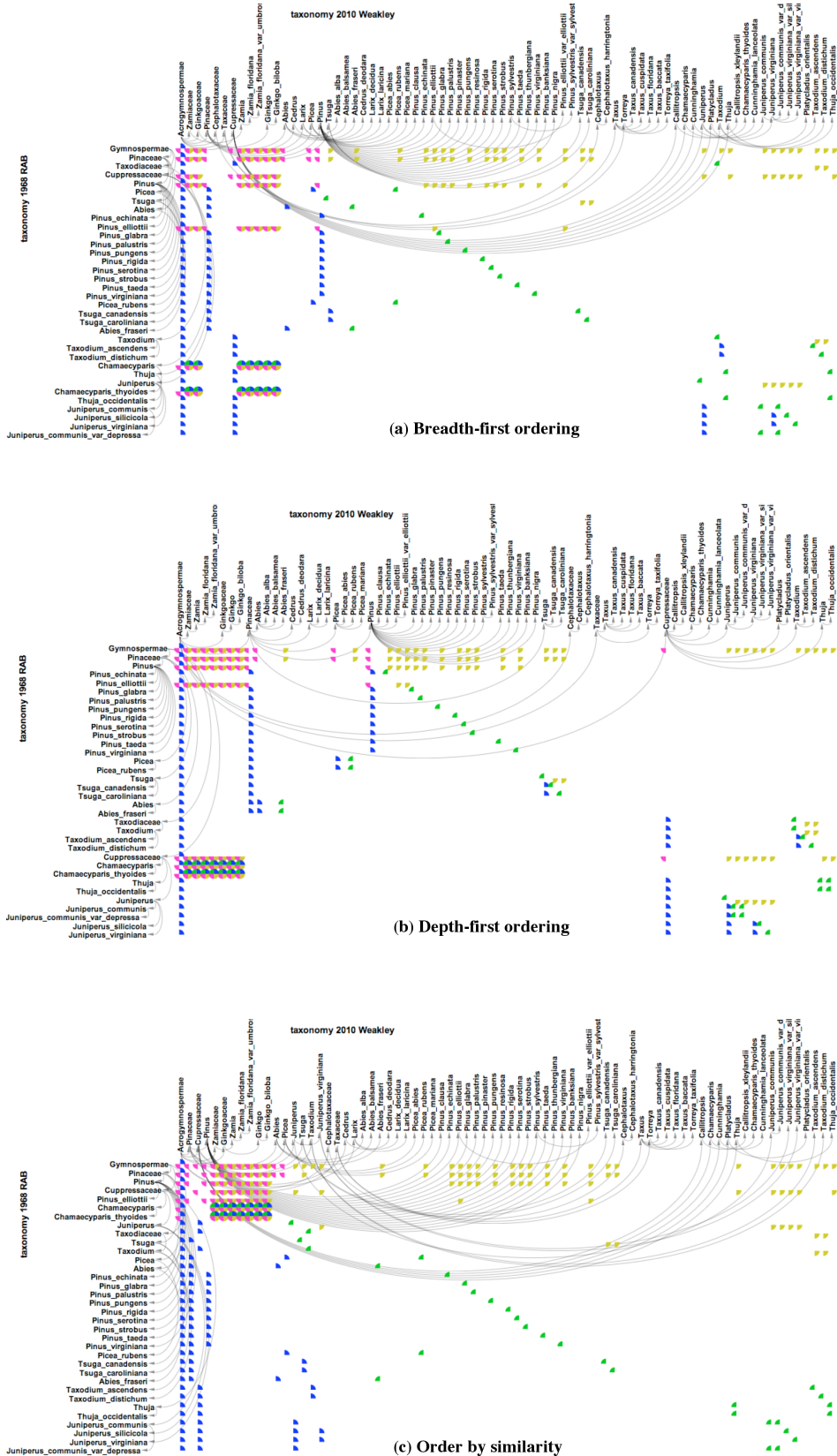
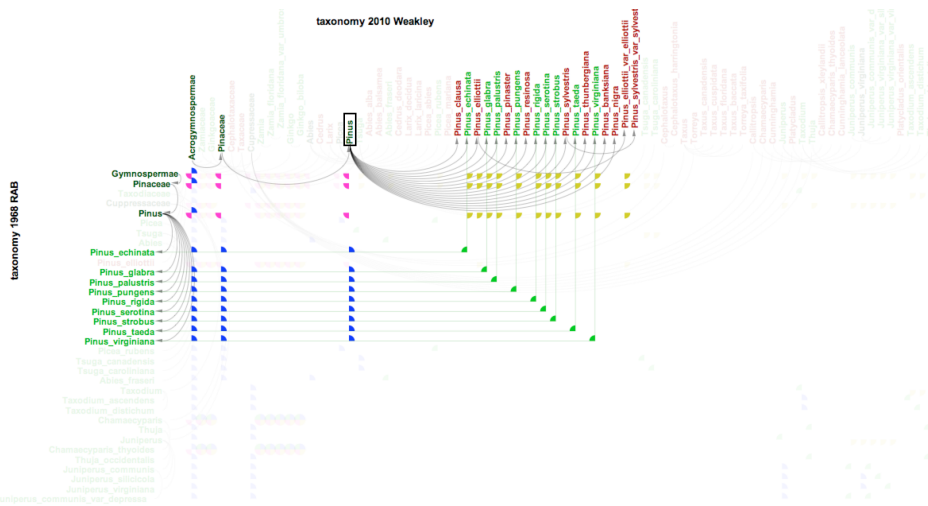


Fig. 4. Visualizing the alignment of Gymnospermae sec. Weakley (2010) vs. RAB (1968) [9]: (a) Breadth-first ordering (b) Depth-first ordering (c) Order by similarity.

variously congruent subtrees, some of which have matching entities in the other taxonomy. Such parent-level concepts are the dark green entities in Figure 5.

- A concept has at least one congruent relationship with a concept in the other taxonomy. Such concepts are highlighted in green.

In Figure 5, we also show brushing and linking to highlight the corresponding subtrees of the aligned taxonomic classifications (**T4**). An associated subtree is discovered based on the presence of congruent relationships which are connected by green lines. In this example, the associated subtree (on the left) of *Pinus* sec. 2010/1968 (in the box) is discovered in light of its aligned children, not the selected (higher-level) taxonomic concept itself. Notice that half of the children (in red) of *Pinus* sec. Weakley (2010) have no congruent match in the RAB (1968) classification.

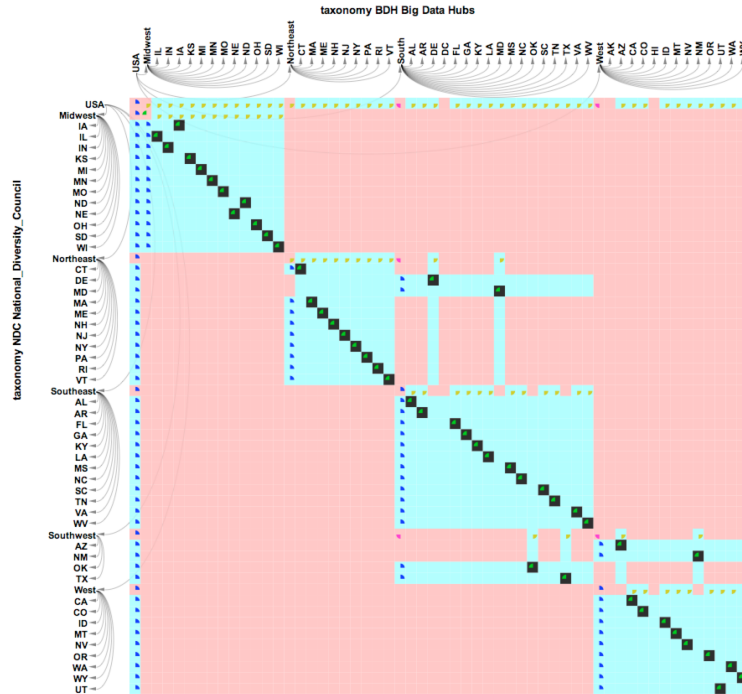


**Fig. 5.** Brushing *Pinus* sec. 2010/1968 in the Gymnospermae use case [9]. Red are incongruent concepts, dark green are incongruent but (some of) the children are congruent, green are congruent.

Additional information and sample images (e.g., from Wikipedia pages of which may entail taxonomic concept information) can be displayed on demand when mousing over a taxonomic concept label (**T5**). Moreover, users can request to overlay the source of articulations (i.e., user input, reasoner inference). Figure 6 shows an example of overlaying such articulation sources in a non-domain demonstration alignment of U.S. regional classifications from National the Diversity Council and Big Data Hubs, respectively. In particular, black cells indicate user input whereas light blue and pink cells are deduced and inferred articulations. Notice that articulation types (circular sectors) are still visible in each cell.

*ProvenanceMatrix* offers two ways navigate and comprehend larger classifications of hundreds of taxonomic concepts: (a) lensing and (b) collapsing a subtree of the input





**Fig. 6.** Visualizing a non-domain, demonstration alignment of U.S. regional classifications. Black cells are user input whereas light blue and pink cells are deduced and inferred articulations.

hierarchies (**T6**). Figure 7 shows a use case of aligning the Primates sec. Groves (1993) and sec. Groves (2005) that contains 317\*483 taxonomic concepts and hence 153,111 MIR [11]. Figure 7(a) shows lensing on a sub-section of the matrix, where only the concept labels (about 20 labels) in the lensing area are printed out. Figure 7(b) shows collapsing of a section of the input hierarchies. A plus sign appears in front of those taxonomic concept labels which are collapsed. *ProvenanceMatrix* also provides searching capability. When users input a concept name into a textbox, *ProvenanceMatrix* only expands the subtree of the search concept and collapses other irrelevant subtrees. At the same time, only related concepts in the other taxonomic classification are expanded.

The *ProvenanceMatrix* application, source code, and an accompanying video tutorial are available online via our project repository.<sup>2</sup>

## 5 Expert User Feedback

The herein provided use cases were provided by EULER/X user and co-author NMF, whose feedback has driven the optimization of the new visualizations. *ProvenanceMatrix* confers two immediate and new visualization services:

<sup>2</sup> <https://github.com/CreativeCodingLab/ProvenanceMatrix>.

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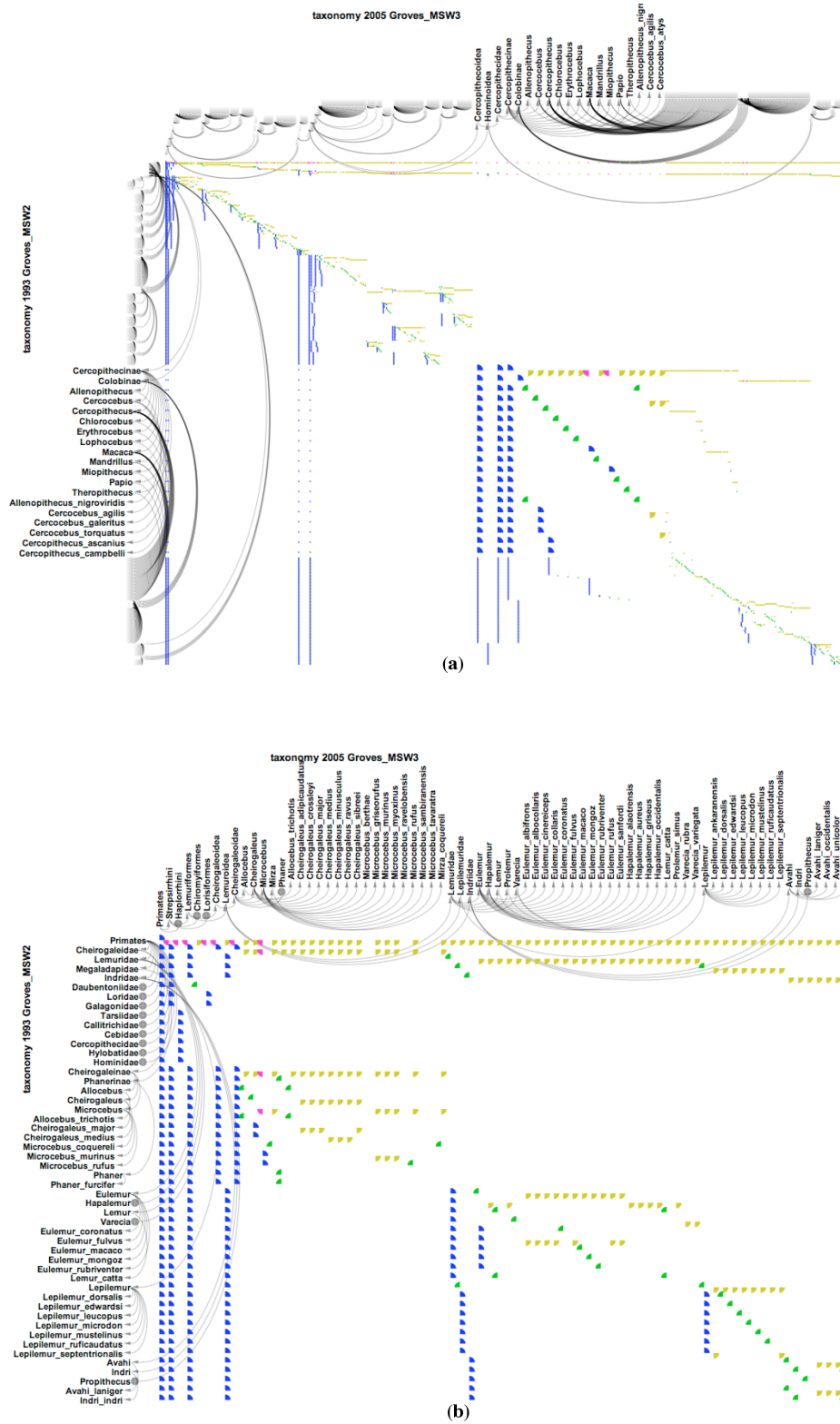


Fig. 7. Visualizing the alignment of two Primates classifications containing 317\*483 taxonomic concepts and 153,111 MIR [11]: (a) lensing on area of interest in the matrix (b) collapsing sub-hierarchies.

(1) In cases where certain concept-to-concept articulations are ambiguous (RCC-5 disjunctions) in the output, the corresponding concepts can be spatially aggregated and thus identified very easily by the user. This can lead to an accelerated understanding and subsequent removal of the ambiguity issues. Without the visualization, one has to instead “comb through” a spreadsheet that may contain many thousands of rows of data. We have succeeded in scaling *ProvenanceMatrix* to this level, even with 153,111 articulations in the Primates sec. 2005/1993 use case [11].

(2) We can show “information expression” that is newly acquired through the EULER/X toolkit reasoning process. For instance, in the Primates use case the expert user provided 402 pairwise input articulations. The reasoning process produces from this 153,111 pairwise MIR relations, i.e., about 380 times as many articulations are logically implied by the input but were not explicitly stated therein. The differential levels of information expression before and after the reasoning process are correspondingly visualized with *ProvenanceMatrix* through two matrix versions, and thus show the powers of the reasoning approach.

In summary, *ProvenanceMatrix* provides speedy and interactive identification of ambiguous input and newly inferred output information, presenting a major improvement over existing visualizations.

## 6 Conclusion and Future Work

This paper introduces a novel technique, *ProvenanceMatrix*, for visualizing the products of a multi-taxonomy alignments generated with the reasoning toolkit EULER/X. Using *ProvenanceMatrix*, users (taxonomists, ecologists, phylogeneticists) can visualize alignments of large taxonomies with up to hundreds of input concepts. Glyphs in each cell highlight RCC-5 articulations for a pair of taxonomic concepts. *ProvenanceMatrix* supports a range of desirable user interactions, such as filtering the matrix by articulations, ordering taxonomic entities with respect to the structure of the input hierarchies, brushing and linking concepts, and collapsing/expanding sub-hierarchies. We have demonstrated how our application effectively facilitates the exploration of multi-taxonomy alignments with different levels of alignment ambiguity and varying sizes, from a few to hundreds of taxonomic entities (and hundreds of thousands of relationships). This technique can be extended to visualize more than two taxonomic classifications – a feature in development for the corresponding reasoning toolkit. In particular, we can have multiple input classifications aligned by rows and columns, where each pair of taxonomic classifications forms a new *ProvenanceMatrix*. In other words, we can create a matrix of *ProvenanceMatrix* matrices, where each cell contains a matrix (similar to the idea of a scatterplot matrix). Future work will investigate this strategy to enable multi-dimensional alignments.

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